# Adaptive Neural Signal Detection for Massive MIMO

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## **Motivation**

• Learning based MIMO detection algorithms have been proposed recently, such as **DetNet** and **OAMPNet**, and they are showing potential.

- However, **neither** approach is effective in practice.
  - DetNet's training is unstable for realistic channels.
  - OAMPNet suffers a large performance gap (4-7dB at symbol error rate of 10^-3).

• Can a receiver optimize its detector for **every realization** of the channel matrix?

# Key Ideas

- It uses a **neural network** architecture that strikes a balance between flexibility and complexity.
  - DetNet is too large for online training
  - OAMPNet performs poorly with online learning infrastructure.

• An online training algorithm that exploits the locality of channel matrices at receiver in both **frequency** and **time** domain.



Received vector:

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n}$$

The channel matrix **H** is assumed known, and the goal is:

$$\hat{\mathbf{x}} = arg \ min_{x \in \mathcal{X}^{N_t}} ||\mathbf{y} - \mathbf{H}\mathbf{x}||_2$$

And it's an NP-hard problem.

## **Iterative Framework for MIMO Detection**

This paper proposes that many MIMO detection algorithms can be transformed into an iterative form: Residual error from the last round.

$$\mathbf{z}_{t} = \hat{\mathbf{x}}_{t} + \mathbf{A}_{t} (\mathbf{y} - \mathbf{H} \hat{\mathbf{x}}_{t}) + \mathbf{b}_{t}$$
  
 $\hat{\mathbf{x}}_{t+1} = \overline{\eta_{t}} (\mathbf{z}_{t})$  Transformation in this round for estimation refinement.

Denoiser

$$(\mathbf{A}_t, \mathbf{b}_t, \mathbf{y} - \mathbf{H}\hat{\mathbf{x}}_t)$$

$$\hat{\mathbf{x}}_t \quad \mathbf{z}_t \quad \mathbf{x}_{t+1} \quad \mathbf{x}_{t+1}$$

# **Optimal Denoiser for Gaussian Noise**

Input is  $\mathbf{z}_t$ , output is  $\hat{\mathbf{x}}_{t+1}$ , we want the final  $\hat{\mathbf{x}}$  to be as close to  $\mathbf{x}$  as possible.

$$arg\,min_{\eta_0,...,\eta_M}\mathbb{E}[||\hat{\mathbf{x}}-\mathbf{x}||_2|\mathbf{z}_0,\ldots,\mathbf{z}_{M+1}]$$

For each specific denoiser, we want:

$$arg\,min_{\eta_t}\mathbb{E}[||\hat{\mathbf{x}}-\mathbf{x}||_2|\mathbf{z}_t]$$

So the output of the denoiser should be:

 $\mathbb{E}[||\mathbb{E}[\mathbf{x}] - \mathbf{x}||_2] = 0$ 

$$\eta_t(\mathbf{z}_t) = \mathbb{E}[\mathbf{x}|\mathbf{z}_t]$$

# **Optimal Denoiser for Gaussian Noise**

If we assume that  $\mathbf{z}_t - x$  has an i.i.d. Gaussian distribution with diagonal covariance matrix  $\sigma_t^2 \mathbf{I}_{N_t}$ , each element of the output should be  $\mathbb{E}[x_i|z]$ .

 $z-x_i \sim N(0,\sigma_t)$ 

$$x_i \sim N(z,\sigma_t)$$

So the output of the denoiser should be

$$\beta_t(z;\sigma_t^2) = \frac{1}{Z} \sum_{x_i \in \mathcal{X}} x_i \exp\left(-\frac{\|z - x_i\|^2}{\sigma_t^2}\right)$$

$$Z = \sum_{x_j \in \mathcal{X}} \exp\left(-\frac{\|z - x_j\|^2}{\sigma_t^2}\right)$$

## **DetNet and OAMPNet**

DetNet:

$$egin{aligned} \mathbf{q}_t &= \hat{\mathbf{x}}_{t-1} - heta_t^{(1)} \mathbf{H}^H \mathbf{y} + heta_t^{(2)} \mathbf{H}^H \mathbf{H} \hat{\mathbf{x}}_{t-1} \ \mathbf{u}_t &= [\Theta_t^{(3)} \mathbf{q}_t + \Theta_t^{(4)} \mathbf{v}_{t-1} + heta_t^{(5)}]_+ \ \mathbf{v}_t &= \Theta_t^{(6)} \mathbf{u}_t + heta_t^{(7)} \ \hat{\mathbf{x}}_t &= \Theta_t^{(8)} \mathbf{u}_t + heta_t^{(9)} \end{aligned}$$

OAMPNet:

$$egin{aligned} \mathbf{z}_t &= \hat{\mathbf{x}}_t + heta_t^{(1)} \mathbf{H}^H (v_t^2 \mathbf{H} \mathbf{H}^H + \sigma^2 \mathbf{I})^{(-1)} (\mathbf{y} - \mathbf{H} \hat{\mathbf{x}}_t) \ & \hat{\mathbf{x}}_{t+1} &= \eta_t ig(\mathbf{z}_t; \sigma_t^2ig) \end{aligned}$$

# MMNet Design – i.i.d. Gaussian Channel

The model is

$$(\mathbf{A}_{t}, \mathbf{b}_{t}, \mathbf{y} - \mathbf{H}\hat{\mathbf{x}}_{t})$$

$$\hat{\mathbf{x}}_{t} \rightarrow \boxed{\text{linear}} \xrightarrow{\mathbf{z}_{t}} \frac{\hat{\mathbf{x}}_{t+1}}{\text{denoiser}} \xrightarrow{\hat{\mathbf{x}}_{t+1}}$$

$$\mathbf{z}_t = \hat{\mathbf{x}}_t + heta_t^{(1)} \mathbf{H}^H (\mathbf{y} - \mathbf{H} \hat{\mathbf{x}}_t)$$

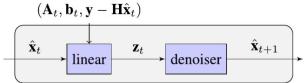
The denoiser is

$$\hat{\mathbf{x}}_{t+1} = \eta_t(\mathbf{z}_t; \sigma_t^2) \hspace{1cm} \mathbf{A}_t \,=\, heta_t^{(1)} \mathbf{H}^H$$

$$\sigma_t^2 = \frac{\theta_t^{(2)}}{N_t} \left( \frac{\|\mathbf{I} - \mathbf{A}_t \mathbf{H}\|_F^2}{\|\mathbf{H}\|_F^2} \left[ \|\mathbf{y} - \mathbf{H}\hat{\mathbf{x}}_t\|_2^2 - N_r \sigma^2 \right]_+ + \frac{\|\mathbf{A}_t\|_F^2}{\|\mathbf{H}\|_F^2} \sigma^2 \right)$$

# MMNet Design – i.i.d. Arbitrary Channel

The model is



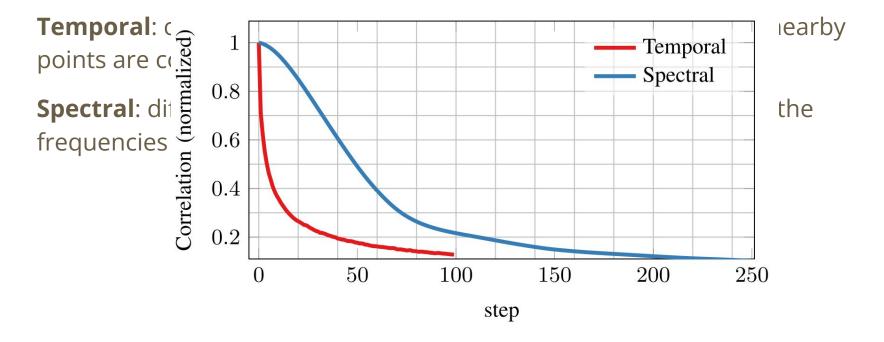
$$\mathbf{z}_t = \hat{\mathbf{x}}_t + \Theta_t^{(1)} (\mathbf{y} - \mathbf{H} \hat{\mathbf{x}}_t)$$

The denoiser is

$$\hat{\mathbf{x}}_{t+1} = \eta_t(\mathbf{z}_t; \sigma_t^2) \hspace{1cm} \mathbf{A}_t = \mathbf{\Theta}_t^{(1)}$$

$$\boldsymbol{\sigma}_{t}^{2} = \frac{\boldsymbol{\theta}_{t}^{(2)}}{N_{t}} \left( \begin{array}{c} \frac{\|\mathbf{I} - \mathbf{A}_{t}\mathbf{H}\|_{F}^{2}}{\|\mathbf{H}\|_{F}^{2}} \left[ \|\mathbf{y} - \mathbf{H}\hat{\mathbf{x}}_{t}\|_{2}^{2} - N_{r}\sigma^{2} \right]_{+} \\ + \frac{\|\mathbf{A}_{t}\|_{F}^{2}}{\|\mathbf{H}\|_{F}^{2}}\sigma^{2} \right)$$

# **Online Training – Channel Locality to Reduce Complexity**



Both forms of channel locality reduce the cost of training.

	Algorithm 1 MMNet online training
<b>Online Trai</b>	1: $\mathcal{M} \leftarrow \text{Construct MMNet with parameters } \vartheta = (2^{(1)} \circ 2^{(2)})^T$
	$\{oldsymbol{\Theta}_t^{(2)},oldsymbol{ heta}_t^{(2)}\}_{t=1}^I$
	2: $\vartheta \leftarrow$ Initialize model parameters randomly
	B: for $n \in \{1, 2,\}$ do $\triangleright n$ keeps the time step n is the interval that the
	4. for $f \in \{1, 2, \dots, F\}$ do channel stays the same,
	5: $\mathbf{H}[f] \leftarrow \text{Measured channel at time step } n \text{ and fre-}$
	quency f
	6: #TrainIterations $\leftarrow$ Set to $\Phi$ if $f \neq 1$ and $\Psi$ otherwise
	$\Phi = 3 - 10 \Psi - 1000$
	7: for it $\in \{1, 2, \dots, \#$ TrainIterations $\}$ do
	8: $\mathbf{D} \leftarrow \text{Generate random } (\mathbf{x}, \mathbf{y}) \text{ batch on } \mathbf{H}[f] \text{ using}$
	(1)
	9: $L \leftarrow$ Find the loss in (15) for $\mathcal{M}$ over the samples
	in <b>D</b>
	10: $\vartheta \leftarrow \text{Compute the model updates using } \nabla_{\vartheta} L$
	11: end for
	12: $\mathcal{M}_n[f] \leftarrow \mathcal{M}.copy() \qquad \triangleright$ Store the parameters $\vartheta$
	13: end for
	14: end for

## **Computational Complexity**

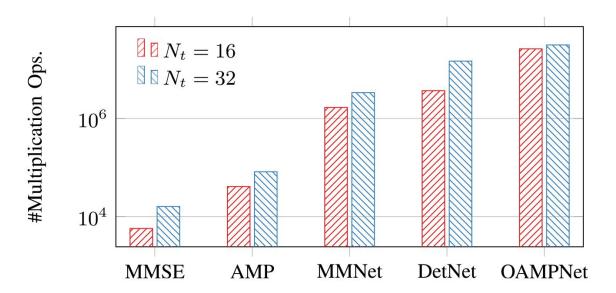
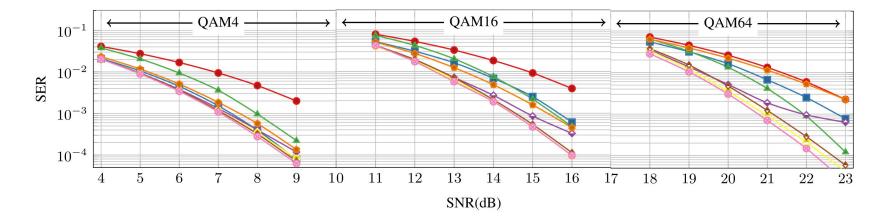
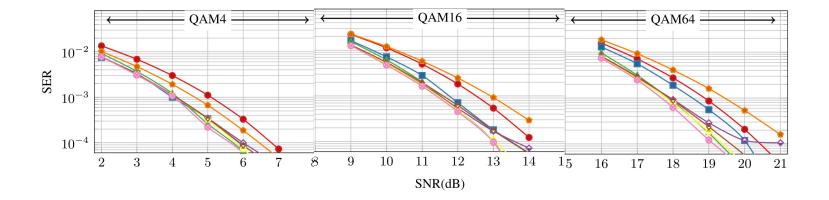


Fig. 12. Number of multiplication operations per signal detection for different algorithms on QAM16 with  $N_r = 64$  receive antennas in 3GPP MIMO model. Detection with MMNet, including its online training process, requires fewer multiplication operations than detection with pre-trained DetNet and OAMPNet models.

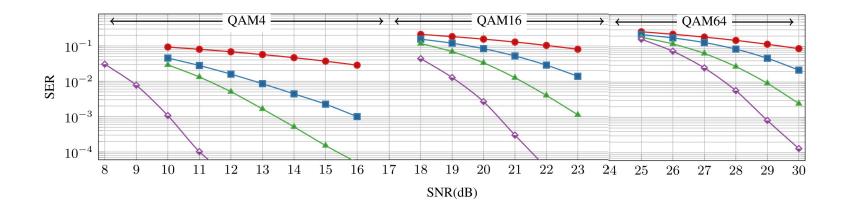
## **Result – i.i.d. Gaussian Channels**



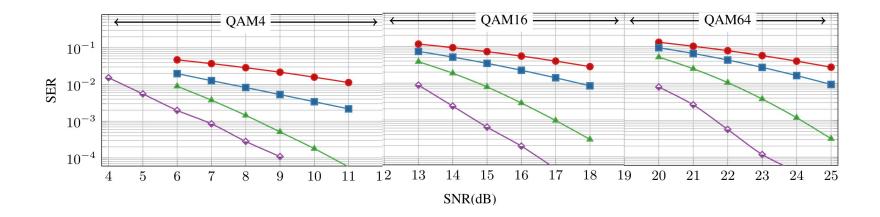
## **Result – i.i.d. Gaussian Channels**



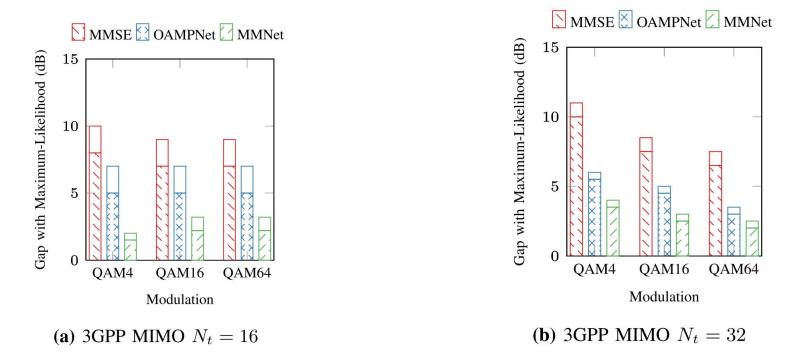
#### **Result – Realistic Channel**



### **Result – Realistic Channel**



# **SNR Gap from the Maximum Likelihood**



To achieve a 10<sup>-3</sup> SER, how much more SNR the methods require, compared with ML

### **Robustness from Channel Estimation Errors**

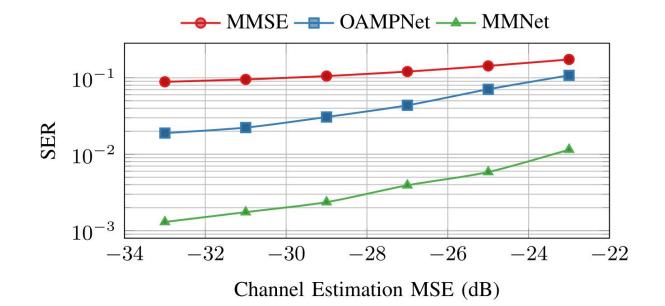
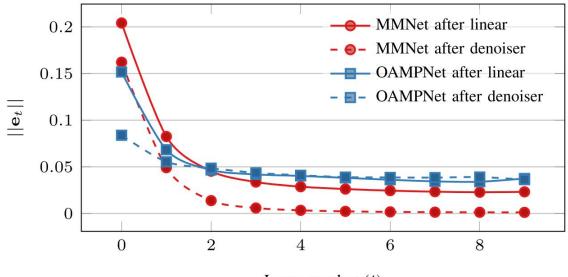


Fig. 5. SER for QAM16 versus channel estimation MSE.

# **Why MMNet Works**



Layer number (t)

Fig. 6. Noise power after the linear and denoiser stages at different layers of OAMPNet and MMNet. The OAMPNet denoisers become ineffective after the third layer on 3GPP MIMO channels.



This paper is well-developed in structure and the resource (GPU) it requires is well-fit in this generation (compared with the next generation Quantum methods).

The online training method considers both effectiveness and the actual deployment computational burden, which is good.

The structure of this paper is a bit of weird – they put the online training section way behind, which could help us understand if it's in earlier section.



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